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[45] Nov. 8, 1983

[54]	DECODERS FOR FEEDING IRREGULAR
	LOUDSPEAKER ARRAYS

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[21] Appl. No.:

305,623

[22] PCT Filed:

Feb. 12, 1981

[86] PCT No.:

PCT/GB81/00018

§ 371 Date:

Sep. 24, 1981

§ 102(e) Date:

Sep. 24, 1981

g 102(c) Date.

Зер. 24, 1901

[87] PCT Pub. No.:

WO81/02502

PCT Pub. Date: Sep. 3, 1981

[30] Foreign Application Priority Data

Feb. 23, 1980 [GB] United Kingdom 8006174

[51] Int. Cl.³ H04R 5/04

[51] Int. Cl. Ho4R 5/04 [52] U.S. Cl. 381/22

[58] Field of Search 179/1 GD, 1 GQ

[56]

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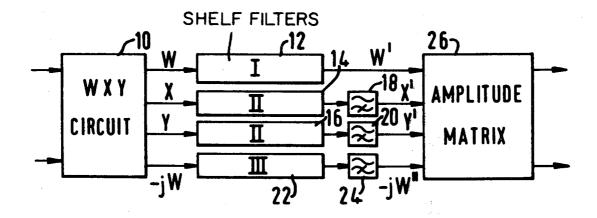
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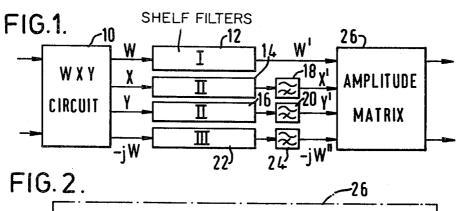
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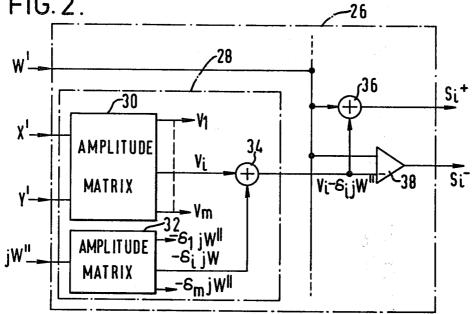
ABSTRACT

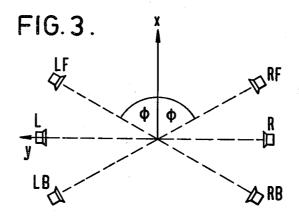
A decoder is provided for feeding an irregular array of m (being three or more) pairs of diametrically opposite loudspeakers, each loudspeaker being disposed at an equal distance r from a common reference point. The decoder incorporates a WXY circuit 10 for producing output signals W, X, Y and -jW from the input signals, and shelf filters 12, 14, 16 and 22 and high-pass filters 18, 20 and 24 for producing output signals W', X', Y' and $-iW_i''$. In addition the decoder includes an amplitude matrix circuit 26 for producing signals S_i ⁺ and S_i ⁻, to be fed to the loudspeakers of each pair, which satisfy particular gain requirements, whereby the outputs of the loudspeakers are adapted to irregular positioning of the loudspeakers which may be dictated by room geometry. A decoder is also provided for feeding a three-dimensional loudspeaker layout.

24 Claims, 7 Drawing Figures









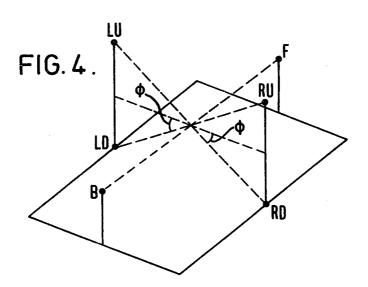
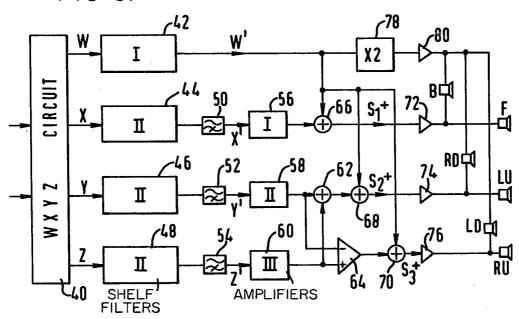
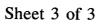


FIG. 5.





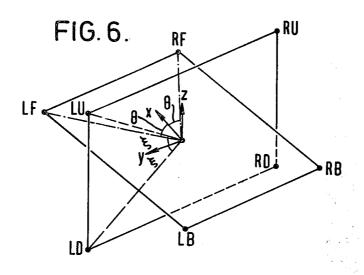
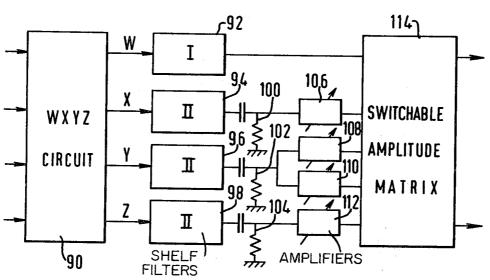


FIG. 7.



DECODERS FOR FEEDING IRREGULAR LOUDSPEAKER ARRAYS

This invention relates to sound reproduction systems and more particularly to sound reproduction systems which enable a listener to distinguish sound from sources extending over 360° of azimuth. Such systems are hereinafter called surround sound systems. The invention is also applicable to surround sound systems which, in addition, enable the listener to distinguish sound from sources at different heights.

Surround sound systems for loudspeaker arrays in which the loudspeakers are disposed at the corners of a geometrically regular polygon, or, in the case of withheight surround sound systems, the corners of a regular solid, are already known. Such systems are also known for loudspeaker arrays where the loudspeakers are disposed to corners of a rectangle or rectangular cuboid. The present invention is concerned with the provision of a decoder for use in a surround sound system where the loudspeakers are disposed at other locations. Such loudspeaker arrays will hereinafter be referred to as irregular loudspeaker arrays and it should be understood that this term excludes rectangular and rectangular cuboid arrays in spite of the fact that these are, in strict mathematical terms, not regular shapes.

It has already been proposed in U.K. Pat. No. 1,411,994 to feed each loudspeaker of an irregular array with a signal having an effective directional pick-up characteristic for encoded sounds which points in the direction of that loudspeaker. However, the results achieved with irregular arrays are not psychoacoustically correct.

Two important theories of sound localisation are the "Makita" theory and the "energy vector" theory. The "Makita" theory is applicable to frequencies less than 700 Hz and has some applicability up to about 1500 Hz. According to this theory, for a loudspeaker array with n loudspeakers all placed at the same distance r from a central reference point at positions indicated by respective rectangular cartesian co-ordinates (x_i, y_i, z_i) where $i=1, 2, \ldots, n$, the localisation of the sound fed to these loudspeakers, where g_i is the complex gain of the sound emerging from the ith loudspeaker, is given by:

$$w = \sum_{i=1}^{n} g_i \tag{1}$$

$$x_{o} = Re\left\{ \left(\sum_{i=1}^{n} g_{i} x_{i} \right) / rw \right\}$$
 (2)

$$y_0 = Re\left\{ \left(\sum_{i=1}^n g_i y_i \right) / rw \right\}$$
 (3)

$$z_{o} = Re\left(\left(\sum_{i=1}^{n} g_{i} z_{i} \right) / rw \right)$$
(4)

where "Re" means "the real part of" and (x_0, y_0, z_0) is a 60 vector pointing to the apparent localisation of the sound with respect to the origin of the cartesian co-ordinates.

For frequencies in the range from approximately 700 Hz to 5 kHz, the "energy vector" theory of localisation is appropriate, the apparent sound direction being the 65 direction of the vector sum of a set of vectors, one pointing to each loudspeaker with a respective length equal to the energy gain of the sound at that loud-

speaker. Then, with a loudspeaker array as described above, the energy vector localisation is the direction of the vector (x_E, y_E, z_E) given by:

$$x_E = \begin{pmatrix} \sum_{i=1}^n |g_i|^2 x_i \end{pmatrix} / \begin{pmatrix} \sum_{i=1}^n |g_i|^2 r \end{pmatrix}$$
 (5)

$$y_E = \begin{pmatrix} \sum_{i=1}^n |g_i|^2 y_i \end{pmatrix} / \begin{pmatrix} \sum_{i=1}^n |g_i|^2 r \end{pmatrix}$$
(6)

$$Z_E = \begin{pmatrix} n \\ \sum_{i=1}^{n} |g_i|^2 z_i \end{pmatrix} / \begin{pmatrix} n \\ \sum_{i=1}^{n} |g_i|^2 r \end{pmatrix}$$
 (7)

The present invention is concerned with the provision of a decoder for an irregular loudspeaker layout which satisfies both the "Makita" and the "energy vector" theories.

According to the invention, there is provided a decoder for feeding an irregular array (as hereinbefore defined) of m (being three or more) pairs of diametrically opposite loudspeakers, each loudspeaker being disposed substantially at an equal distance r from a common reference point, comprising an amplitude matrix circuit so arranged that, in operation, the sum of the signals S_i^+ and S_i^- fed to the loudspeakers of each pair is the same for all pairs of loudspeakers, and such that, if the ith pair of loudspeakers has cartesian coordinates (x_i, y_i, z_i) and $(-x_i, -y_i, -z_i)$ with respect to rectangular cartesian axes x, y and z at the reference point,

$$S_i^+ = W' + \alpha_i X' + \beta_i Y' + \gamma_i Z' - \delta_i j W_i''$$

$$S_i^- = W' - \alpha_i X' - \beta_i Y' - \gamma_i Z' + \delta_{ij} W_i''$$

where W' is a signal representative of the acoustical pressure at the reference point and is independent of i, X', Y' and Z' are signals representative of the components of a desired acoustical velocity along the x, y and z axes and are independent of i.

 jW_i " is any signal bearing a 90° phase relationship to W' for all encoded sound directions, and

 α_i , β_i , γ_i , and δ_i are real gain coefficients such that α_i , β_i , and γ_i substantially satisfy the following matrix equation:

$$KM = \frac{k mr I}{\sqrt{2}}$$

where K is the $m \times 3$ matrix:

$$\begin{pmatrix} x_1 & x_2 & x_m \\ y_1 & y_2 & \cdots & y_m \\ z_1 & z_2 & z_m \end{pmatrix}$$

M is the 3 \times m matrix of coefficients:

$$\begin{pmatrix} \alpha_1 & \beta_1 & \gamma_1 \\ \alpha_2 & \beta_2 & \gamma_2 \\ \vdots \\ \alpha_m & \beta_m & \gamma_m \end{pmatrix}$$

I is the identity matrix:

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$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \text{ for a three-dimensional loudspeaker layout}$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \text{ for a two-dimensional horizontal loudspeaker layout,}$$

and k is a positive real constant which may be frequency and energy vector localisations always coincide.

It should be understood that, although jWi" may be the same for all pairs of diametrically opposite loudspeakers, this signal may also differ for different loudspeaker pairs provided that each signal bears a 90° phase 20 relationship to W' for all encoded sound directions.

When the invention is to be applied to a decoder having a "WXY" circuit, as described in U.K. Pat. No. 1,494,751, having outputs W, X, Y such that the intended direction of sound localisation is an azimuth $\boldsymbol{\varphi},\ 25$ measured anticlockwise from the x-axis, where:

$$\cos\phi:\sin\phi = Re(X/W): Re(Y/W)$$
 ...(8)

then a decoder in accordance with the invention for 30 feeding an irregular horizontal array of loudspeakers consisting of m diametrically opposite pairs of loudspeakers (where m is 3 or more) produces signals to be fed to the loudspeakers of each pair given by Si_i ⁺ and S_i^- , where i = 1, 2, ..., m and $S_i^+ = W' + \alpha_i X' + \beta_i Y' - \delta_{ij} W_i''$

$$S_i^+ = W' + \alpha_i X' + \beta_i Y' - \delta_{ij} W_i'' \qquad (9)$$

$$S_i^- = W' - \alpha_i X' - \beta_i Y' + \delta_{ij} W_i'' \qquad \qquad \dots (10)$$

where α_i , β_i and δ_i are real gains, arranged such that the 40 apparent sound localisation according to Makita's theory is substantially equal to the aximuth ϕ . It will be understood that, in equation (8), the convention has been used of letting the symbols W, X and Y representing signals also denote the complex gains of these sig- 45 nals for a given single encoded sound direction.

If desired, the gains of the signals W, X and Y may be altered provided that the gains in the X and Y channels are identical and the phase responses in all three channels are identical. Gains applied may be frequency- 50 dependent. A fourth signal path is provided for conveying a signal proportional to $-jW_i$ " which is used to apply directional biasing as described in U.K. Patent No. 1,550,627, the biasing signals applied to the loudspeakers of each pair being of equal magnitude but 55 opposite polarity.

Embodiments of the invention will now be described by way of example with reference to the accompanying drawings, in which:

FIG. 1 is a block schematic diagram of a decoder for 60 a horizontal surround sound decoder in accordance with the invention,

FIG. 2 is a block schematic diagram of part of an amplitude matrix for the decoder shown in FIG. 1,

FIG. 3 shows an irregular hexagonal loudspeaker 65 array suitable for use with the decoder shown in FIG. 1,

FIG. 4 shows an irregular octahedral loudspeaker array,

FIG. 5 is a block schematic diagram of a decoder in accordance with the invention for use with the loudspeaker array shown in FIG. 4,

FIG. 6 is an irregular three dimensional array of eight 5 loudspeakers, and

FIG. 7 is a block schematic diagram of a decoder in accordance with the invention for use with a loudspeaker array as shown in FIG. 4 or 6.

Referring to FIG. 1, a decoder for a horizontal sur-10 round sound system has a WXY circuit 10 arranged to receive coded input signals and produce output signals W, X and Y. In addition, the circuit 10 produces a second output W phase-shifted by 90° to give the signal dependent. It can be shown that the condition S_i^++- -jW. The signal W is applied to a type I shelf filter 12 $S_i^-=2W$ for all i is sufficient to ensure that the Makita 15 to produce the signal W'. The signals X and Y are applied to respective type II shelf filters 14 and 16 and respective high-pass filters 18 and 20 to produce the signals X' and Y', and the signal -jW is applied to a type III shelf filter 22 and a high-pass filter 24 to produce the signal -jW". The shelf filters 12, 14 and 16 have substantially identical phase responses, and are used to achieve a different ratio of velocity to pressure information at the reference listening position at low frequencies, for example less than 400 Hz, and at high frequency, for example greater than 700 Hz. The highpass filters 18, 20 and 24 are used to compensate for curvature of the sound field due to finite loudspeaker distance and optimally have their -3 dB points at a frequency (53/r) Hz where r is the distance of the loudspeakers from the reference point in meters. The signal -jW" is used to apply directional biasing. The nature and functions of the various filters 12 to 24 is more fully described in U.K. Pat. Nos. 1,494,751, 1,494,752 and 1,550,627.

The signals W', X', Y', -jW'' are applied to an amplitude matrix 26. Referring to FIG. 2, the matrix 26 comprises a 3 × m amplitude matrix 28, to which the signals X', Y' and -jW'' are applied and which produces m outputs, $V_1 - \delta_1 j W''$ to $\hat{V}_m - \delta_m j W''$, one for each pair of loudspeakers. The matrix 28 comprises a 2 ×m amplitude matrix 30, to which the signals X' and Y' are applied and which produces m outputs V_1 to V_m , a $1 \times m$ amplitude matrix 32, to which the signal $-jW^{\prime\prime}$ is applied and which produces m directional biasing signals $-\delta_{1j}W''$ to $-\delta_{mj}W''$, and m addition circuits 34 for adding $-\delta_{ij}W''$ to V_i to produce a respective signal $V_i - \delta_{ij}W''$ for each pair of loudspeakers, where the real coefficients δ_i are chosen to achieve the desired degree of directional biasing. In addition, the matrix 26 includes an addition circuit 36 and a subtraction circuit 38 for each pair of loudspeakers of which only the circuits for the ith loudspeaker pair are shown in FIG. 2. The signal W' and the output $V_i - \delta_{ij}W''$ are applied to the addition circuit 36, the output of which comprises the signal:

$$S_i^+ = W + V_i - \delta_j W' \qquad (11)$$

and forms a feed signal for one of the loudspeakers of the ith pair. The signal W' is also applied to the positive input of the subtractor 38 and the signal $V_i - \delta_i j W''$ from the amplitude matrix 34 is applied to the negative input thereof, the output of which is given by:

$$S_i = W - V_i + \delta_{ij}W' \qquad \qquad (12)$$

and forms the feed signal for the other loudspeaker of the ith pair.

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It will be understood that, if no directional biasing is required, then $\delta_i = 0$ for every i, and that in that case all parts of the circuit of FIG. 1 and FIG. 2 concerned with the handling of the signal -jW may be omitted. Also, it will be understood that any amplitude matrix producing 5 outputs identical to those of the circuit 26 falls within the scope of the invention, and that, in particular, it may often by convenient to perform the addition of the bias signal -jW" prior to the amplitude matrix 28 rather than subsequent to it.

Since the amplitude matrix 28 having matrix coefficients such that:

$$V_i = \alpha_i X' + \beta_i Y \tag{13}$$

is required to satisfy Makita localisation criteria of 25 Equation (8), the coefficients α_i and β_i of the matrix must satisfy the equations:

$$\sum_{i=1}^{m} \alpha_i x_i = \sum_{i=1}^{m} \beta_i y_i = mr/\sqrt{2}$$
(15)

$$\sum_{i=1}^{m} \alpha_{i} y_{i} = \sum_{i=1}^{m} \beta_{i} x_{i} = 0$$
 (16)

Since $S_i^+ + S_i^- = 2W'$ for such an amplitude matrix, 35 it also follows that the energy vector localisation coincides with the Makita localisation for this amplitude matrix.

If we write the $2 \times m$ matrix of the coefficients:

$$\begin{pmatrix} \alpha_1 \, eta_1 \\ \vdots \\ \alpha_m \, eta_m \end{pmatrix}$$

of the matrix 28 as M and the $m \times 2$ matrix

$$\begin{pmatrix} x_1 & x_m \\ & \ddots & \\ y_1 & y_m \end{pmatrix}$$

as K, then the Equations 15 and 16 can be rewritten in matrix form as:

$$KM = \frac{1}{\sqrt{2}} mrI \tag{17}$$

where I is the 2×2 identity matrix and r is the distance of the loudspeakers from the reference listening position as before.

In practice, any positive real multiple k of the matrix M satisfying Equation 17 may be used, that is one can 65 multiply all gains α_i , β_i by a fixed positive gain k. However, it is preferable to use a multiple k of M which also ensures the condition:

$$k^{2}\{(Re(X'/W'))^{2}+(Re(Y'/W'))^{2}\}=2$$
 ...(18)

is satisfied, since, if this condition is met, not only the Makita theory, but also other low frequency localisation theories are satisfied. This last mentioned condition is satisfied, for example, when W' has unity gain for all sounds, and X' has gain $\sqrt{2}\cos\theta$ and Y' has gain $\sqrt{2}\sin\theta$ θ for a sound originating from an azimuth θ measured 10 anticlockwise from the front direction and when k equals 1.

The constant k may be implemented by means of gain or shelf filter circuits affecting the signals X', Y' and W' prior to the final output matrix circuitry, and additional 15 changes of gain, phase response and frequency response may be applied to these signals, provided that all the signals are affected equally by these additional changes.

A convenient way of devising a matrix M satisfying the condition:

$$KM = \frac{k}{\sqrt{2}} mrI \tag{19}$$

, and therefore giving correct localisation, is as follows. For each pair of loudspeakers:

$$\begin{pmatrix} \alpha_i \\ \beta_i \end{pmatrix} = \frac{k}{\sqrt{2}} mr \begin{pmatrix} m \\ \sum_{h=1}^{m} \begin{pmatrix} x_h^2 x_h y_h \\ x_h y_h y_h^2 \end{pmatrix} \end{pmatrix}^{-1} \begin{pmatrix} x_i \\ y_i \end{pmatrix}$$
(20)

where the power -1 indicates a matrix inverse.

The application of Equation 20 to the irregular hexagonal loudspeaker array shown in FIG. 3 will now be described. The array of FIG. 3 consists of a due left loudspeaker L, a due right loudspeaker R and four loudspeakers LB, LF, RF and RB placed at respective azimuths $180^{\circ} - \phi$, ϕ , $-\phi$, and $-180^{\circ} + \phi$ measured anticlockwise from due front. Putting due front as the x direction, due left as the y direction and S_1^+ , S_2^+ , S_3^+ , S_1^{1-} , S_2^{-} , S_3^{-} equal to the signals fed to the respective loudspeakers LB, L, LF, RF, R, RB we have:

$$(x_1, y_1) = (-r\cos\phi, r\sin\phi)$$
 (21)
 $(x_2, y_2) = (0, r)$ (22)
 $(x_3, y_3) = (r\cos\phi, r\sin\phi)$ (23)

$$(x_2, y_2) = (0, r)$$

$$(x_3, y_3) = (r\cos\phi, r\sin\phi)$$

$$(23)$$

$$\begin{pmatrix} \alpha_i \\ \beta_i \end{pmatrix} = \frac{3r^{-1}k}{\sqrt{2}} \begin{pmatrix} 2\cos^2\phi & 0 \\ 0 & 1 + 2\sin^2\phi \end{pmatrix}^{-1} \begin{pmatrix} x_i \\ y_i \end{pmatrix}$$
(24)

$$=\frac{r^{-1}k}{\sqrt{2}}\begin{pmatrix} \frac{3}{2\cos^2\phi} & 0\\ 0 & \frac{3}{1+2\sin^2\phi} \end{pmatrix} \begin{pmatrix} x_i\\ y_i \end{pmatrix}$$

From Equation 24:

$$M = \begin{pmatrix} \alpha_1 \, \beta_1 \\ \alpha_2 \, \beta_2 \\ \alpha_3 \, \beta_3 \end{pmatrix} = \frac{k}{\sqrt{2}} \begin{pmatrix} \frac{-3}{2\cos\phi} & \frac{3\sin\phi}{1 + 2\sin^2\phi} \\ 0 & \frac{3}{1 + 2\sin^2\phi} \\ \frac{3}{2\cos\phi} & \frac{3\sin\phi}{1 + 2\sin^2\phi} \end{pmatrix}$$
(25)

and the amplitude matrix 28 is FIGS. 1 and 2 feeds the following signals to the loudspeakers of FIG. 3:

$$S_1^+ = W' - \frac{3k}{2\sqrt{2}\cos\phi}X' + \frac{3k\sin\phi}{\sqrt{2}(1+2\sin^2\phi)}Y'^{(26)}$$

$$S_2^+ = W + \frac{3k}{\sqrt{2} (1 + 2\sin^2\phi)} Y \tag{27}$$

$$S_3^+ = W + \frac{3k}{2\sqrt{2}\cos\phi} X' + \frac{3k\sin\phi}{\sqrt{2}(1+2\sin^2\phi)} Y'$$
 (28)

$$S_1^- = W + \frac{3k}{2\sqrt{2}\cos\phi} X' - \frac{3k\sin\phi}{\sqrt{2}(1+2\sin^2\phi)} Y$$
 (29)

$$S_2^- = W = \frac{3k}{\sqrt{2} (1 + 2\sin^2\phi)} Y \tag{30}$$

$$S_3^- = W - \frac{3k}{2\sqrt{2} \cos \phi} X - \frac{3k \sin \phi}{\sqrt{2} (1 + 2\sin^2 \phi)} Y^{(31)}$$

The matrix coefficients of the amplitude matrix 30 20 may have any real value chosen to provide the required directional biasing, if any, or alternatively directional biasing may be achieved by modifying the signals X' and Y' as described in above-mentioned U.S. Pat. No. 1,550,627.

It should be understood that, in all these decoders, the signals X and Y from the WXY circuit 10 may be replaced by two independent real linear combinations of X and Y provided that the amplitude matrix 26 derives from these linear combinations the required output signals S_i^+ and S_i^- . Moreover, matrices may be combined or rearranged in the circuitry wherever this is of design or constructional convenience so that a part of the output amplitude matrix function might, for example, be combined with the function of the WXY circuit.

It will be appreciated that the gains α_1 , α_2 and α_3 , β_1 , β_2 and β_3 of the above decoder for a hexagonal loud-speaker layout depend on the angle ϕ , and that it will often be desirable to incorporate means for providing a continuous adjustment of the value of ϕ in the decoder circuit. To this end the gains $\alpha_1 = -\alpha_3$ (which result in a signal component $\alpha_1 X' = -\alpha_3 X'$) may be implemented by a first variable gain circuit placed in the X' signal path, the gain β_2 (which results in a signal component $\beta_2 Y'$) may be implemented by a second variable gain circuit placed in the Y' signal path, and the gains $\beta_1 = \beta_3$ (which result in a signal component $\beta_1 Y' = \beta_3 Y'$) may be implemented by a third variable gain circuit placed in the Y' signal path. Simultaneous adjustment of these three variable gain circuits will then 50 permit the decoder to be adapted to loudspeaker layouts with various different values of ϕ .

The invention may also be applied to irregular threedimensional loudspeaker arrays where the loudspeakers are placed in m diametrically opposite pairs at a distance r from the reference listening point. In the following discussion it is assumed that the ith of m pairs of loudspeakers have positions given by the cartesian coordinates (x_i, y_i, z_i) and $(-x_i, -y_i, -z_i)$ and are fed with respective signals S_i^{30} and S_i^{-} . W, X, Y and Z are 60 signals representative respectively of the desired pressure and x-axis, y-axis, and z-axis components of velocity of sound at the reference listening position. Such signals may be subjected to shelf filters having identical phase responses and to RC high-pass filters compensating for loudspeaker distance, analogous to the filters described with reference to FIG. 1, provided only that the filtering on each of the X, Y and Z signal paths is

identical, producing modified signals W', X', Y', Z'. Then, in accordance with the invention, the Makita and energy vector localisation give the same direction of sound provided that:

$$S_i^+ + S_i^+ = 2W$$
 for $i = 1, 2, ..., m$... (32)

In addition, it is often desired that this localisation be at the direction of the point (Re (X/W), Re (Y/W), Re 10 (Z/W)), and in that case the signals S_i^+ and S_i^- are given by:

$$S_i^+ = W' + \alpha_i X' + \beta_i Y' + \gamma_i Z' - \delta_i j W_i^{"} \qquad \qquad \dots (33)$$

$$S_i^+ = W' - \alpha_i X' - \beta_i Y' - \gamma_i Z' + \delta_{ij} W_i'' \qquad \qquad \dots (34)$$

where α_i , β_i , γ_i and δ_i are real coefficients, where jW'' is any signal having a 90° phase relation to W' for all sound directions, and where the $3 \times m$ matrix:

$$M = \begin{pmatrix} \alpha_1 \, \beta_1 \, \gamma_1 \\ \alpha_2 \, \beta_2 \, \gamma_2 \\ \vdots \\ \alpha_m \, \beta_m \, \gamma_m \end{pmatrix}$$
(35)

satisfies the matrix equation:

$$KM = \frac{1}{\sqrt{2}} kmrI \tag{36}$$

where k is a positive constant and

$$K = \begin{pmatrix} x_1 \dots x_m \\ y_1 \dots y_m \\ z_1 \dots z_m \end{pmatrix}$$
 (37)

and I is the 3×3 identity matrix and where δ_i are the arbitrary real coefficients of directional biasing signals. The Equation (36) may alternatively be written as:

$$\sum_{i=1}^{m} \alpha_i x_i = \sum_{i=1}^{m} \beta_i y_i = \sum_{i=1}^{m} \gamma_i z_i = \frac{kmr}{\sqrt{2}}, \sum_{i=1}^{m} \alpha_i y_i = \sum_{i=1}^{m} \alpha_i z_i =$$

$$\sum_{i=1}^{m} \beta_i x_i = \sum_{i=1}^{m} \beta_i z_i = \sum_{i=1}^{m} \gamma_i x_i = \sum_{i=1}^{m} \gamma_i y_i = 0.$$

In particular, the matrix M may be given by the equation:

$$\begin{pmatrix} a_i \\ \beta_i \\ \gamma_i \end{pmatrix} = \frac{1}{\sqrt{2}} kmr \left\{ \begin{array}{l} m \\ \sum \\ k = 1 \\ k = 1 \end{array} \begin{pmatrix} x_h^2 & x_h y_h & x_h z_h \\ x_h y_h & y_h^2 & y_h z_h \\ x_h z_h & y_h z_h & z_h^2 \end{array} \right\}^{-1} \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}$$

A matrix M satisfying Equation 36 yields correct localisation according to all major low frequency localisation theories provided that the constant k is chosen to ensure that:

$$k^{2}\{(Re(X'/W'))^{2}+(Re(Y'/W'))^{2}+(Re(Z'/W'))^{2}\}=2$$
 (39)

for encoded sounds.

The constant k may be implemented by means of gain or shelf filter circuits affecting the signals X', Y', Z' and

W' prior to the final output matrix circuitry, and additional changes of gain, phase response and frequency response may be applied to these signals, provided that all the signals are affected equally by these additional changes.

For horizontally encoded sounds, Z=0, in which case the Z signal path may be omitted, and the system reduces to that previously described with reference to FIGS. 1 and 2, except that the values of α_i and β_i may be somewhat altered in accordance with Equation 36.

FIG. 4 indicates an irregular octahedral layout of six loudspeakers F, B, LU, LD, RU and RD placed at a distance r from a reference point and respectively disposed in front, behind, at an angle ϕ above due left, at an angle ϕ below due left, at an angle ϕ above due right, and at an angle ϕ below due right. The corresponding loudspeaker feed signals S_1^+ , S_1^- , S_2^+ , S_3^- , S_3^+ , S_2^+ , are fed to the loudspeakers at \pm (x_i , y_i , z_i) where:

$$(x_1, y_1, z_1) = (r, 0.0)$$
 (40) 20
 $(x_2, y_2, z_2) = (0, r \cos\phi, r \sin\phi)$
 $(x_3, y_3, z_3) = (0, -r \cos\phi, r \sin\phi)$

Use of the above-mentioned matrix Formula 38 gives: 25

$$\begin{pmatrix} \alpha_{1} \beta_{1} \gamma_{1} \\ \alpha_{2} \beta_{2} \gamma_{2} \\ \alpha_{3} \beta_{3} \gamma_{3} \end{pmatrix} = \frac{k}{\sqrt{2}} \begin{pmatrix} 3 & 0 & 0 \\ 0 & \frac{3}{2 \cos\phi} & \frac{3}{2 \sin\phi} \\ 0 - \frac{3}{2 \cos\phi} & \frac{3}{2 \sin\phi} \end{pmatrix}$$
(41)

so that the loudspeaker feed signals are:

$$S_{1}^{+} = W' + \frac{3k}{\sqrt{2}} X'$$

$$S_{1}^{-} = W' - \frac{3k}{\sqrt{2}} X'$$

$$S_{2}^{+} = W' + \frac{3k}{2\sqrt{2}\cos\phi} Y' + \frac{3k}{2\sqrt{2}\sin\phi} Z'$$

$$S_{2}^{-} = W' - \frac{3k}{2\sqrt{2}\cos\phi} Y' - \frac{3k}{22\sin\phi} Z'$$

$$S_{3}^{+} = W' - \frac{3k}{2\sqrt{2}\cos\phi} Y' + \frac{3k}{2\sqrt{2}\sin\phi} Z'$$

$$S_{3}^{-} = W' + \frac{3k}{2\sqrt{2}\cos\phi} Y' - \frac{3k}{2\sqrt{2}\sin\phi} Z'$$

FIG. 5 illustrates a decoder for use in the case when the signal W has unit gain for sounds encoded from all 55 directions in space, and where X, Y and Z have respective gains $\sqrt{2}\cos\theta\cos\eta$, $\sqrt{2}\sin\theta\cos\eta$ and $\sqrt{2}\sin\eta$ for sounds having source azimuth θ measured anticlockwise from due front and source elevation measured upwards from horizontal such as may occur in the decoders of certain four-channel encoding systems with full-sphere directionality. The signals W, X, Y and Z are produced from the received input signals by a WXYZ circuit 40. The W signal is applied to a type I shelf filter 42 while the X, Y and Z signals are applied to respective 65 type II shelf filters 44, 46 and 48. The function of the shelf filters 42 to 48 is analogous to that of shelf filters 12, 14 and 16 of FIG. 1 and the transition frequency

between low and high frequency gains is preferably centred at about 350 Hz, the shelf filters of both types having unity gain at low frequencies while the type I shelf filter has gain $\sqrt{2}$ and the type II shelf filters have gain $\sqrt{\frac{2}{3}}$ at frequencies well above the transition frequencies. The ratio of gains of the type II shelf filters to the type I shelf filter may be considered to implement a part of the factor k referred to in Equations (41) and (42). In this case it will be seen that k is a frequency dependent gain. The X, Y and Z signal paths also include High-pass filters 50, 52 and 54 to compensate for sound field curvature due to finite loudspeaker distance as previously described.

The X, Y and Z signal paths also include amplifiers 56, 58 and 60 applying respective gains I, II and III in order to implement matrix Equation 35. For the loud-speaker layout of FIG. 4, these gains are given by:

gain
$$I = \frac{3}{\sqrt{2}}$$

gain $II = \frac{3}{2\sqrt{2} \cos\phi}$
gain $III = \frac{3}{2\sqrt{2} \sinh\phi}$

The output signals in the Y and Z channels from the amplifiers 58 and 60 respectively are added by an addition circuit 62 to give the difference signals for the LU and RD pair of loudspeakers, and subtracted by a subtraction circuit 64 to obtain the difference signal for the RU and LD pair of loudspeakers. The output signal in the X channel, from the amplifier 56, itself constitutes the difference signal for the F and B pair of loudspekers. Each of these differences signals is combined by a respective addition circuit 66, 68 and 70 to give the signals S₁+, S₂+, and S₃+which are amplified by respective power amplifiers 72, 74 and 76 and fed through the loudspeakers F, LU and RU.

The output signal in the W channel from the shelf filter 42 is also applied to an amplifier 78 having a gain of 2 and thence to a power amplifier 80 having equal gain to that of the power amplifiers 72, 74 and 76. Each of the signals S₁+, S₂+, and S₃+is subtracted from the output of the amplifier 80 by connecting a respective one of the loudspeakers B, RD and LD between the output of the amplifier 80 and the output of the corresponding one of the amplifiers 72, 74 and 76. Thus only four power amplifiers are needed to feed the six loudspeakers. This so-called loudspeaker matrixing technique forms the subject of U.K. Pat. No. 1,548,674 and may also be applied to decoders for feeding horizontal loudspeaker arrays in accordance with the present invention, such as the decoder illustrated in FIGS. 2 and 3. It is often desirable to incorporate variable gain means for matching a range of loudspeaker arrangements by adjusting the gains of the signals X', Y' and Z' before they are fed to the matrix circuit. A first variable gain circuit may be provided for multiplying the signal X' by the gain coefficient α_1 , a second variable gain circuit may be provided for multiplying the signal Y' by the gain coefficients β_2 and β_3 , and a third variable gain circuit may be provided for multiplying the signal Z' by the gain coefficients γ_2 and γ_3 .

It will be appreciated that other spatial orientations of the octahedral layout of FIG. 4 may be used, provided that the signals X, Y and Z are matrixed or interchanged to correspond to components of sound velocity along the reorientated spatial axes.

The invention may also be applied to more complex irregular loudspeaker layouts. For example, the invention may be applied to a three dimensional layout of eight loudspeakers LF, RF, LB, RB, LU, LD, RU and RD as shown in FIG. 6, placed at the cartesian co-ordinates (x_i, y_i, z_i) and $(-x_i, -y_i, -z_i)$ with respective feed signals S_i + and S_i - of the form given in Equations (33) 10 and (34), where i has the values 1 to 4, and where, for radius r:

$$(x_1, y_1, z_1) = (r\cos\phi, r\sin\phi, o)$$

$$(x_2, y_2, z_2) = (r\cos\phi, -r\sin\phi, o)$$

$$(x_3, y_3, z_3) = (o, r\cos\xi, r\sin\xi)$$

$$(x_4, y_4, z_4) = (0, -r\cos\xi, r\sin\xi)$$

$$(44)$$

This corresponds to a loudspeaker layout consisting of a combination of a horizontal array of four loudspeakers with an angle 2ϕ subtended at the centre by the front loudspeaker pair, and a vertical rectangular array of four loudspeakers with an angle 2ξ subtended at the centre by one of the vertical loudspeaker pairs.

Such a loudspeaker layout can be made to satisfy the directional requirements of the Makita and energy vector theories if one applies Equation (38) to the layout. A calculation then shows that:

$$\begin{pmatrix} \alpha_1 \, \beta_1 \, \gamma_1 \\ \alpha_2 \, \beta_2 \, \gamma_2 \\ \alpha_3 \, \beta_3 \, \gamma_3 \\ \alpha_4 \, \beta_4 \, \gamma_4 \end{pmatrix} = \sqrt{2} \ k \begin{pmatrix} 1/\cos\phi & \sin\phi/(\sin^2\phi \, + \, \cos^2\xi) & 0 \\ 1/\cos\phi & -\sin\phi/(\sin^2\phi \, + \, \cos^2\xi) & 0 \\ 0 & \cos\xi/(\sin^2\phi \, + \, \cos^2\xi) & 1/\sin\xi \\ 0 & -\cos\xi/(\sin^2\phi \, + \, \cos^2\xi) & 1/\sin\xi \end{pmatrix}$$

so that the loudspeaker feed signals are given by Equations (33) and (34) by using these values of α_i , β_i , γ_i for 40 a suitable positive gain k (which may be chosen to be frequency dependent).

FIG. 7 illustrates a decoder for use with a variety of three dimensional loudspeaker layouts in accordance with this invention, including those described above in 45 reference to FIGS. 4 and 6. This decoder is also suitable for use with a cuboid of loudspeakers as described in U.K. Patent Nos. 1,494,751 and 1,494,752 and incorporates a WXYZ circuit 90, type I and II shelf filters 92, 94, 96 and 98 and also high-pass filters 100, 102 and 104 50 to compensate for loudspeaker distance as described in the aforementioned specifications. The decoder also incorporates a switchable amplitude matrix 114. By providing several variable gain amplifiers 106, 108, 110 and 112, and by making the output amplitude matrix 55 coefficients switchable to match the type of loudspeaker layout chosen, a single decoder can be made which is suitable for a number of different loudspeaker layouts. In particular, the variable gain amplifiers permit adjustment of the angles $\frac{1}{8}$ and ξ describing the exact 60 shape of the loudspeaker layout and thus act as a "layout control". The variable gain amplifier 106 multiplies the signal X' by the gain coefficients α_1 and α_2 , the variable gain amplifier 108 multiplies the signal Y' by the gain coefficients β_1 and β_2 , the variable gain ampli- 65 fier 110 multiplies the signal Y' by the gain coefficient β_3 and β_4 , and the variable gain amplifier 112 multiplies the signal Z' by the gain coefficients γ_3 and γ_4 .

Any of the decoders described above can be used in conjunction with additional gain and time delay circuitry which serves to modify the output signals from the decoder prior to feeding these to the loudspeakers in order to compensate for loudspeakers at unequal distances from the common reference point, in accordance with the provisions of U.K. Pat. No. 1,552,478.

It will also be appreciated that the designation of the x-axis as being "forward", the y-axis as being "leftward" and the z-axis as being "upward" in this specification is purely arbitrary, and that x, y and z axes could equally as well be chosen to be any other set of 3 orthogonal cartesian axes at the common reference point. Thus, for example, by making the x-axis point leftward and the y-axis point forward, the decoders described with reference to FIGS. 3 to 6 will be suitable for alternative orientations of loudspeaker layouts. Thus, the L loudspeaker of FIG. 3 will become a front loudspeaker, the R loudspeaker will become a back loudspeaker, and the left front, left back, right front, right back loudspeakers will become respectively left front, right front, left back and right back loudspeakers. In a similar way, the octahedral layout of FIG. 4 will consist of front and back vertical pairs of speakers and one loudspeaker at each side. Finally, the layout of FIG. 6 will consist of front and back vertical pairs of loudspeakers and left and right side pairs of loudspeakers.

It will also be appreciated that the amplitude matrix described above may also incorporate any additional overall gain (including phase inversion where appropriate) such as might be considered desirable by one skilled in the art.

I claim:

1. A decoder for feeding an array of m (being three or more) pairs of diametrically opposite loudspeakers, the array being an irregular array, that is an array in which the loudspeakers are disposed in positions other than at the corners of a regular polygon or regular solid or a rectangle or rectangular cuboid, each loudspeaker being disposed substantially at an equal distance r from a common reference point, and the ith pair of loudspeakers having cartesian coordinates (xi, yi, zi) and $(-x_i, -y_i, -z_i)$ with respect to rectangular cartesian axes x, y and z at the reference point, said decoder comprising input means for receiving coded input signals representative of the desired acoustical pressure and velocity at the reference point and for outputting signals W, X, Y and, for a three-dimensional loudspeaker layout, Z, filter means connected to the input means for producing, from said signals W, X, Y, Z, a signal W' representative of the desired acoustical pressure at the reference point and independent of i, signals X', Y' and, where appropriate, Z' representative of the components of the desired acoustical velocity along the x, y and z axes and independent of i, and a signal jW_i " bearing a 90° phase relationship to W' for all encoded sound directions, and an amplitude matrix circuit connected to the filter means for producing, from the output signals of said filter means, signals S_i ⁺ and S_i ⁻ to be fed to the loudspeakers of each pair, the sum of which is the same for all pairs of loudspeakers, where

$$S_i^+ = W + \alpha_i X' + \beta_i Y' + \gamma_i Z' - \delta_{ij} W_i''$$

$$S_i^- = W' - \alpha_i X' - \beta_i Y' - \gamma_i Z' + \delta_{ij} W_i''$$

25

where α_i , β_i , γ_i , and δ_i are real gain coefficients such that α_i , β_i and γ_i substantially satisfy the following matrix equation:

$$KM = \frac{k mr I}{\sqrt{2}}$$

where K is the $m \times 3$ matrix:

$$\begin{pmatrix} x_1 & x_2 & x_m \\ y_1 & y_2 & \cdots & y_m \\ z_1 & z_2 & z_m \end{pmatrix},$$

M is the 3×m matrix of coefficients:

I is the identity matrix:

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \text{ for a three-dimensional loudspeaker}$$
 layout

or

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \text{ for a two-dimensional, horizontal loudspeaker layout,}$$

and k is a positive real constant which may be 40 frequency dependent.

- 2. A decoder according to claim 1, wherein the signal jW_i'' produced by the filter means is the same for all pairs of diametrically opposite loudspeakers.
- 3. A decoder according to claim 1, for a two-dimensional loudspeaker layout, the ith pair of loudspeakers of which has cartesian coordinates (x_i, y_i) and $(-x_i, -y_i)$ with respect to rectangular cartesian axes x and y at the reference point, wherein the amplitude matrix circuit produces signals $S_i^+ = W' + \alpha_i X' + \beta_i Y' \delta_i W_i''$

$$S_i = W' - \alpha_i X' - \beta_i Y' + \delta_i j W_i''$$

where α_i , β_i and δ_i are real gain coefficients such that α_{i-55} and β_i substantially satisfy the following equations:

$$\sum_{i=1}^{m} \alpha_i x_i = \sum_{i=1}^{m} \beta_i y_i = \frac{kmr}{\sqrt{2}}$$

$$\sum_{i=1}^{m} \alpha_i y_i = \sum_{i=1}^{m} \beta_i x_i = 0.$$

4. A decoder according to claim 3, wherein the amplitude matrix circuit produces signals; the gain coefficients α_i and β_i of which are substantially given by the matrix equations:

$$\begin{pmatrix} \alpha_i \\ \beta_i \end{pmatrix} = \frac{1}{\sqrt{2}} kmr \begin{pmatrix} m \\ \sum_{h=1}^{m} \begin{pmatrix} x_h^2 & x_h y_h \\ x_h y_h & y_h^2 \end{pmatrix} \end{pmatrix}^{-1} \begin{pmatrix} x_i \\ y_i \end{pmatrix}$$

where the power -1 indicates the matrix inverse.

- 5. A decoder according to claim 3, wherein the amplitude matrix is such that, considering the signal W' as having unity gain and incorporating encoded sounds from all directions, the signal X' has gain $\sqrt{2} \cos \theta$, and the signal Y' has gain $\sqrt{2} \sin \theta$ for a sound originating from an azimuth θ .
 - 6. A decoder according to claim 3, wherein the filter means incorporates a first shelf filter circuit for producing the signal W', and identical second shelf filter circuits are provided for producing the signals X' and Y'.
- A decoder according to claim 6, wherein the first
 and second shelf filter circuits have substantially identical phase responses at all audio frequencies.
 - 8. A decoder according to claim 3, wherein the amplitude matrix circuit is such as to ensure that the constant k at low frequencies satisfies the equation:

$$k^{2}\{(Re(X'/W'))^{2}+(Re(Y'/W'))^{2}\}=2$$

for all horizontal sounds encoded into the signals W', X' and Y', where Re denotes "the real part of".

9. A decoder according to claim 4, for feeding respective signals S_1^+ , S_1^- , S_2^+ , S_2^- , S_3^+ and S_3^- to an irregular arrangement of six loudspeakers placed at the cartesian coordinates $\pm (x_i, y_i)$ where

(x₁, y₁)=
$$(-r\cos\phi, r\sin\phi)$$

(x₂, y₂)= $(0, r)$
(x₃, Y₃)= $(r\cos\phi, r\sin\phi)$

wherein the signals produced by the amplitude matrix circuit satisfy the equation:

$$\begin{pmatrix} \alpha_1 \, \beta_1 \, \gamma_1 \\ \alpha_2 \, \beta_2 \, \gamma_2 \\ \alpha_3 \, \beta_3 \, \gamma_3 \\ \alpha_4 \, \beta_4 \, \gamma_4 \end{pmatrix} = \sqrt{2} \, k \begin{pmatrix} 1/\cos\phi & \sin\phi/(\sin^2\phi + \cos^2\xi) & 0 \\ 1/\cos\phi - \sin\phi/(\sin^2\phi + \cos^2\xi) & 0 \\ 0 & \cos\xi/(\sin^2\phi + \cos^2\xi) & 1/\sin\xi \\ 0 & -\cos\xi/(\sin^2\phi + \cos^2\xi) & 1/\sin\xi \end{pmatrix}$$

- 10. A decoder according to claim 3, wherein the amplitude matrix circuit comprises variable gain means for matching a range of loudspeaker arrangements by adjusting the gains of the signals X' and Y' before they are fed into a fixed matrix circuit.
- 11. A decoder according to claim 9, wherein a first variable gain circuit is provided for multiplying the signal X' by the gain coefficients α_1 and α_3 , a second variable gain circuit is provided for multiplying the signal Y' by the gain coefficient β_2 , and a third variable gain circuit is provided for multiplying the signal Y' by the gain coefficients β_1 and β_3 .
- 12. A decoder according to claim 1, for a three-dimensional loudspeaker layout, wherein the amplitude matrix circuit produces signals such that the gain coefficients α_i , β_i and γ_i substantially satisfy the following equations:

$$\sum_{i=1}^{m}\alpha_{i}x_{i}=\sum_{i=1}^{m}\beta_{i}y_{i}=\sum_{i=1}^{m}\gamma_{i}z_{i}=\frac{kmr}{\sqrt{2}}\;,\;\sum_{i=1}^{m}\alpha_{i}y_{i}=\sum_{i=1}^{m}\alpha_{i}z_{i}=\sum_{i=$$

-continued

$$\sum_{i=1}^{m} \beta_i x_i = \sum_{i=1}^{m} \beta_i z_i = \sum_{i=1}^{m} \gamma_i x_i = \sum_{i=1}^{m} \gamma_i y_i = 0.$$

13. A decoder according to claim 12, wherein the amplitude matrix circuit produces signals such that the gain coefficients α_i , β_i and γ_i are substantially given by the matrix equations:

$$\begin{pmatrix} \alpha_i \\ \beta_i \\ \gamma_i \end{pmatrix} = \frac{1}{\sqrt{2}} kmr \begin{pmatrix} m \\ \sum_{h=1}^{m} \begin{pmatrix} x_h^2 & x_h y_h & x_h z_h \\ x_h y_h & y_h^2 & y_h z_h \\ x_h z_h & y_n z_h & z_h^2 \end{pmatrix} \end{pmatrix}^{-1} \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}$$

where the power -1 indicates the matrix inverse.

- 14. A decoder according to claim 12, wherein the amplitude matrix circuit is such that, considering the signal W' as having unity gain and incorporating sounds from all directions, the signals X', Y' and Z' have gains $\sqrt{2}\cos\theta\cos\eta$, $\sqrt{2}\sin\theta\cos\eta$ and $\sqrt{2}\sin\eta$ for a sound having a source azimuth θ measured anticlockwise from the x-axis and a source elevation η measured upward 25 from the xy-plane to the x-axis.
- 15. A decoder according to claim 12, wherein the filter means incorporates a first shelf filter circuit for producing the signal W' and identical second shelf filter 30 circuits are for producing the signals X', Y' and Z'.
- 16. A decoder according to claim 15, wherein the first and second shelf filter circuits have substantially identical phase responses at all audio frequencies.
- 17. A decoder according to claim 12, wherein the amplitude matrix circuit is such as to ensure that the constant k at low frequencies satisfies the equation:

$$k^{2} \{ (Re(X'/W'))^{2} + (Re(Y'/W'))^{2} + (Re(Z'/W'))^{2} \} = 2$$

for all directional sounds encoded into the signals W', X', Y' and Z'.

- 18. A decoder according to claim 13, for feeding 45 respective signals S_1+ , S_1- , S_2+ , S_2- , S_3+ and S_3- to an irregular arrangement of six loudspeakers placed at the vertices of an irregular octahedron at a distance r from the origin of the cartesian coordinates.
- 19. A decoder according to claim 12, wherein the amplitude matrix circuit comprises variable gain means for matching a range of loudspeaker arrangements by adjusting the gains of the signals X', Y' and Z' before they are fed into a fixed matrix circuit.
- 20. A decoder according to claim 18, wherein the loudspeaker coordinates are $\pm(x_i, y_i, z_i)$ where

$$(x_1, y_1, z_1) = (r, O, O)$$

 $(x_2, y_2, z_2) = (O, r \cos \phi, r \sin \phi)$
 $(x_3, y_3, z_3) = (O, -r \cos \phi, r \sin \phi)$

and the signals produced by the amplitude matrix cir- 65 cuit satisfy the equation:

$$5 \begin{pmatrix} \alpha_1 \, \beta_1 \, \gamma_1 \\ \alpha_2 \, \beta_2 \, \gamma_2 \\ \alpha_3 \, \beta_3 \, \gamma_3 \\ \alpha_4 \, \beta_4 \, \gamma_4 \end{pmatrix} = \sqrt{2} \, k \begin{pmatrix} 1/\cos\phi & \sin\phi/(\sin^2\phi \, + \, \cos^2\xi) & 0 \\ 1/\cos\phi \, - \sin\phi/(\sin^2\phi \, + \, \cos^2\xi) & 0 \\ 0 & \cos\xi/(\sin^2\phi \, + \, \cos^2\xi) & 1/\sin\xi \\ 0 & -\cos\xi/(\sin^2\phi \, + \, \cos^2\xi) & 1/\sin\xi \end{pmatrix}$$

21. A decoder according to claim 19, wherein a first variable gain circuit is provided for multiplying the signal X' by the gain coefficient α₁, a second variable gain circuit is provided for multiplying the signal Y' by the gain coefficient β₂ and β₃, and a third variable gain circuit is provided for multiplying the signal Z' by the gain coefficients γ₂ and γ₃.

22. A decoder according to claim 18, wherein four power amplifiers having one output terminal in common are provided for receiving signals S_1^+ , S_2^+ , S_3^+ , the power amplifiers being connected to the six loud-speakers such that each of the loudspeakers requiring signals S_1^+ , S_2^+ and S_3^+ is driven by a respective amplifier and each of the diametrically opposite loudspeakers requiring signals S_1^- , S_2^- and S_3^- is driven by having one terminal of the loudspeaker coupled to the non-common output terminal of a respective amplifier and the other terminal of the loudspeaker coupled to the non-common output terminal of the amplifier provided for receiving the signal 2W'.

23. A decoder according to claim 13, for feeding respective signals S_1^+ , S_1^- , S_2^+ , S_2^- , S_3^+ , S_3^- , S_4^+ and S_4^- to an irregular arrangement of eight loudspeakers placed at the vertices of a rectangle in the xy-plane and at the vertices of a rectangle in the yz-plane at the cartesian coordinates $\pm (x_i, y_i, z_i)$ where

$$(x_1, y_1, z_1) = (r\cos \phi, r\sin \phi, 0)$$

 $(x_2, y_2, z_2) = (r\cos \phi, -r\sin \phi, 0)$
 $(x_3, y_3, z_3) = (O, r\cos \xi, r\sin \xi)$
 $(x_4, y_4, z_4) = (O, -r\cos \xi, r\sin \xi)$

wherein the signals produced by the amplitude matrix circuit satisfy the equation:

$$\begin{pmatrix} \alpha_1 \, \beta_1 \, \gamma_1 \\ \alpha_2 \, \beta_2 \, \gamma_2 \\ \alpha_3 \, \beta_3 \, \gamma_3 \\ \alpha_4 \, \beta_4 \, \gamma_4 \end{pmatrix} = \sqrt{2} \, k \begin{pmatrix} 1/\cos\phi & \sin\phi/(\sin^2\phi + \cos^2\xi) & 0 \\ 1/\cos\phi - \sin\phi/(\sin^2\phi + \cos^2\xi) & 0 \\ 0 & \cos\xi/(\sin^2\phi + \cos^2\xi) & 1/\sin\xi \\ 0 & -\cos\xi/(\sin^2\phi + \cos^2\xi) & 1/\sin\xi \end{pmatrix}$$

24. A decoder according to claim 23, adjustable for a range of values of the angles ϕ and ξ , wherein the amplitude matrix circuit comprises adjustment means for matching a range of loudspeaker arrangements by adjusting the gains of the signals X', Y' and Z' before they are fed into a fixed matrix circuit, and wherein a first variable gain circuit is provided for multiplying the signal X' by the gain coefficients α_1 and α_2 , a second variable gain circuit is provided for multiplying the signal Y' by the gain coefficients β_1 and β_2 , a third variable gain circuit is provided for multiplying the signal Y' by the gain coefficients β_3 and β_4 , and a fourth variable gain circuit is provided for multiplying the signal Z' by the gain coefficients γ_3 and γ_4 .